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**Statistical methods for  
implementation of Six Sigma —  
Selected illustrations of contingency  
table analysis**

*Méthodes statistiques pour l'implémentation de Six Sigma —  
Exemples sélectionnés d'application de l'analyse de tableau de  
contingence*



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## Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see [www.iso.org/directives](http://www.iso.org/directives)).

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights. Details of any patent rights identified during the development of the document will be in the Introduction and/or on the ISO list of patent declarations received (see [www.iso.org/patents](http://www.iso.org/patents)).

Any trade name used in this document is information given for the convenience of users and does not constitute an endorsement.

For an explanation on the meaning of ISO specific terms and expressions related to conformity assessment, as well as information about ISO's adherence to the World Trade Organization (WTO) principles in the Technical Barriers to Trade (TBT) see the following URL: [www.iso.org/iso/foreword.html](http://www.iso.org/iso/foreword.html).

The committee responsible for this document is ISO/TC 69, *Applications of statistical methods*, Subcommittee SC 7, *Applications of statistical and related techniques for the implementation of Six Sigma*.

## Introduction

The Six Sigma and international statistical standards communities share a philosophy of continuous improvement and many analytical tools. The Six Sigma community tends to adopt a pragmatic approach driven by time and resource constraints. The statistical standards community arrives at rigorous documents through long-term international consensus. The disparities in time pressures, mathematical rigor, and statistical software usage have inhibited exchanges, synergy, and mutual appreciation between the two groups.

The present document takes one specific statistical tool (Contingency Table Analysis), develops the topic somewhat generically (in the spirit of International Standards), then illustrates it through the use of several detailed and distinct applications. The generic description focuses on the commonalities across studies designed to assess the association of categorical variables.

The Annexes containing illustrations do not only follow the basic framework, but also identify the nuances and peculiarities in the specific applications. Each example will offer at least one “winkle” to the problem, which is generally the case for real Six Sigma and other fields application.



# Statistical methods for implementation of Six Sigma — Selected illustrations of contingency table analysis

## 1 Scope

This document describes the necessary steps for contingency table analysis and the method to analyse the relation between categorical variables (including nominal variables and ordinal variables).

This document provides examples of contingency table analysis. Several illustrations from different fields with different emphasis suggest the procedures of contingency table analysis using different software applications.

In this document, only two-dimensional contingency tables are considered.

## 2 Normative references

There are no normative references in this document.

## 3 Terms and definitions

For the purposes of this document, the terms and definitions given in ISO 3534-1 and ISO 3534-2 and the following apply.

ISO and IEC maintain terminological databases for use in standardization at the following addresses:

- IEC Electropedia: available at <http://www.electropedia.org/>
- ISO Online browsing platform: available at <http://www.iso.org/obp>

### 3.1

#### **categorical variable**

variable with the measurement scale consisting of a set of categories

### 3.2

#### **nominal data**

variable with a nominal scale of measurement

[SOURCE: ISO 3534-2:2006, 1.1.6]

### 3.3

#### **ordinal data**

variable with an ordinal scale of measurement

[SOURCE: ISO 3534-2:2006, 1.1.7]

### 3.4

#### **contingency table**

tabular representation of categorical data, which shows frequencies for particular combinations of values of two or more discrete random variables

Note 1 to entry: A table that cross-classifies two variables is called a “two-way contingency table;” the one that cross-classifies three variables is called a “three-way contingency table.” A two-way table with  $r$  rows and  $c$  columns is also named “ $r \times c$  table.”

EXAMPLE Let  $n$  items be classified by categorical variables  $X$  and  $Y$  with levels  $X_1, X_2$  and  $Y_1, Y_2$ , respectively. The number of items with both attribute  $X_i$  and  $Y_j$  is  $n_{ij}$ . Then, a  $2 \times 2$  table is as follows.